Empirics of Financial Markets

Major issues – a review

Coverage

• Empirical models with some theoretical contents

Detailed list of issues covered (1/2)

- Equity market: explaining normal returns : CAPM and its extensions, APT)
- Financial markets at large: what explains prices and yields – random walk, efficient market hypothesis
- Financial markets at large: volatility modelling (ARCH/GARCH models)

Detailed list of issues covered (2/2)

- Fixed income (debt) market: yield curve modelling (term structures of interest rates)
- FX market: basic theories of exchange rate level and dynamics, market microstructure

CAPM and APT (1/4)

 Systematic (non-diversifiable) risk (*interest rates, business cycle*) vs.
unsystematic (idiosyncratic) risk (*change* of tax structure favoring some industries)

 Major hypothesis: expected yield is a linear function of a covariance between that yield and market yield.

CAPM and APT (2/4)

• Empirical formula: OLS

$$R_{it} = \alpha_i + \beta_i R_{mt} + \varepsilon_{it}$$

- CAPM testing:
 - Intercept equals 0;
 - $-\beta$ is the only factor explaining yield differences.
- Two-stage estimation procedure (lab)

CAPM and APT (3/4)

- Problems of CAPM:
 - Market portfolio unobservable
 - Number of factors too low ->APT popularity

CAPM and APT (4/4)

- APT: allows many (not identified by the model) factors, does not require a market portfolio
- Law of one price: portfolios with the same factor sensitivities should have the same yield
- Empirical model: OLS

Random walk

• (1900 r.) the oldest concept in quantitative finance

$$\Delta P_t = \mu + \mathcal{E}_t$$

- Random walk hypotheses:
 - RW1 any functions of the increments are uncorrelated
 - RW2 independent increments (but not their functions)
 - RW3 uncorrelated increments

Efficient Market Hypothesis (1/2)

- Efficiency may mean different things: allocative efficiency, transactional efficiency, informational efficiency...
- EMH: stock prices fully and correctly reflect all relevant information [Fama (1970)].

$$\mathsf{P}_{t+1} = \mathsf{E}[\mathsf{P}_{t+1} | \mathsf{I}_t] + \varepsilon_{t+1}$$

• Weak, semi-strong and strong efficiency

EMH (2/2)

- Weak efficiency:
 - I includes past prices.
 - Technical analysis cannot bring abnormal returns

• Semi-strong efficiency:

- I includes all public information
- Both fundamental and technical analysis cannot bring abnormal returns
- Strong efficiency:
 - I includes all (also private) information (*inside information*).
 - Insider trading cannot bring abnormal returns.

Volatility Modelling (ARCH/GARCH) (1/4)

- Background: Routine volatility models assumed homogenous error term - for most financial data error term variance usually varies upon time!
- Explicit variance modelling gives better volatility estimates and forecasts

Volatility Modelling (ARCH/GARCH) (2/4)

- Stylized facts:
 - -Leptokurtic distribution
 - -Variance clustering
 - Leverage effect (a negative correlation between past returns and future volatility)

Volatility Modelling (ARCH/GARCH) (3/4)

• ARCH(q)

$$\sigma_t^2 = \alpha_0 + \alpha_1 u_{t-1}^2 + \dots + \alpha_q u_{t-q}^2$$

- For a positive variance parameters estimates have to be positive
- A large number of parameters to be estimated
- GARCH(p,q)

$$\sigma_t^2 = \alpha + \alpha_1 u_{t-1}^2 + \dots + \alpha_q u_{t-q}^2 + \beta_1 \sigma_{t-1}^2 + \dots + \beta_2 \sigma_{t-p}^2$$

- Parsimonious specification
- Problems with a leverage effect

Volatility Modelling (ARCH/GARCH) (4/4)

• ARCH-in-mean

 Allow for higher premia tied to higher risk (shown in data)

• GARCH-t

- Fat tails in distribution of residuals

Yield Curve (1/3)

- Yield curve depicts formally a term structure of interest rates
- Types of yield curve shape :
 - normal
 - flat
 - inverted
 - humped

Yield Curve (2/3)

- Theoretical background :
 - Expectation theory
 - Liquidity preference theory
 - Market segmentation theory
 - Preferred habitat theory

Yield Curve (3/3)

- Nelson-Siegel model
- Svensson model

Forex market

- Purchasing power parity (PPP) (absolute, relative)
- Interest rate parity (covered, uncovered)

• Monetary models

• Market microstructure